

Brief Articles

A Swift All-Atom Energy-Based Computational Protocol to Predict DNA–Ligand Binding Affinity and ΔT_m

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A hybrid molecular mechanics–statistical mechanics–solvent accessibility-based computational protocol is developed to calculate DNA–ligand binding affinity without any database training and is validated on 50 DNA–ligand complexes. The calculated binding energies yield high correlation coefficients of 0.95 ($R^2 = 0.90$) and 0.96 ($R^2 = 0.93$) in linear plots against experimental binding free energies (ΔG°) and ΔT_m , respectively. The protocol is translated into a swift, web-enabled, freely accessible computational tool, <http://www.scfbio-iitd.res.in/preddicta>, for ΔG° and ΔT_m prediction for DNA–ligand complexes to aid and expedite rational drug design attempts.

Introduction

Energetics provides a vital link between structure and function of molecular systems. Correlating structural features with binding affinities allows the design of better binders via structure based drug design methods.¹ Thus, a computational tool that can determine the binding affinity accurately and expeditiously is of immediate value in drug design endeavors.

DNA is an important anticancer/antibiotic drug target, and recent years have seen an increasing number of ligands being designed to target specific DNA sequences, notable among which are polyamides, bi-benzimidazole derivatives, bisanthracyclines, bisfuramidines, and the more recent biarylpyrimidines (citations to original literature in Supporting Information). Several energy/scoring functions² based on force field, empirical, and knowledge based methods have been reported in literature for protein–ligand, protein–DNA, and protein–protein interactions and widely employed for docking and virtual screening and also for attempting binding affinity prediction,³ but parallel efforts for DNA–ligand systems have begun only recently.⁴ Approaches like MMPBSA and MMGBSA have also been widely employed for binding affinity calculation, but show limited success for DNA–ligand complexes.^{5,6} Thus, for binding affinity predictions and for scoring DNA–ligand complexes, the need for fast and accurate methods persists.

Addressing this concern, we present here a computational methodology and web tool for generating swift estimates of DNA–ligand affinities while maintaining a phenomenological physicochemical approach. The energy function is validated on 50 DNA–ligand complexes containing 16 crystal and 34 model-built structures via linear correlations between theoretically calculated binding energies and experimentally determined binding free energies and ΔT_m (changes in melting, i.e., helix-to-coil transition temperature of DNA on drug binding) values reported in literature.

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Theory

Accurate determination of absolute binding free energies in biomolecular systems,⁷ especially in DNA–ligand complexes, has been a daunting task for computational chemists due to major challenges. First, modeling and simulation⁸ of DNA requires careful consideration of solvent and counterion atmosphere to ensure system stability. Second, evolving a computational technique based on classical and statistical mechanical principles to obtain estimates of binding affinities that correlate well with experiment requires a thorough accounting of all possible energy components and their accurate estimation.⁹ To this end, we propose an energy function, which represents the calculated DNA–ligand binding energy as a combination of electrostatic and steric complementarities as well as entropic and solvent effects, including hydrophobicity, and is expressed as

$$\Delta G^\circ_{\text{cbe}} = \Delta H^\circ_{\text{el}} + \Delta H^\circ_{\text{vdw}} - T\Delta S^\circ_{\text{rt}} + \Delta G^\circ_{\text{w}} \quad (1)$$

Each component in eq 1 is described below.

$\Delta H^\circ_{\text{el}}$, Electrostatic Term. $\Delta H^\circ_{\text{el}}$ includes interactions between partial atomic charges on the DNA and ligand atoms calculated from Coulomb's law, employing a sigmoidal dielectric function¹⁰ for solvent screening and scaled phosphate charges according to Manning theory,¹¹ thus implicitly incorporating desolvation electrostatics and counterion effects. For a single time-averaged crystal/minimized/model-built structure, $\Delta H^\circ_{\text{el}} \approx \Delta E^\circ_{\text{el}}$. For atom i of DNA and j of the ligand

$$E_{\text{el}} (\text{kcal/mol}) = \frac{\sum_i \sum_j 332q_i q_j}{D(r)r_{ij}}$$

where q_i and q_j are the partial atomic charges on atoms i and j , r_{ij} is the i – j distance, $D(r)$ is a sigmoidal dielectric function taken as $D(r) = D - [(\alpha^2 + 2\alpha + 2)e^{-\alpha(D - D_i)}/2]$; $D = 78$; $D_i = 4$; $\alpha = sr$; and $s = 0.395$. Finally, $\Delta H^\circ_{\text{el}} \approx \Delta E^\circ_{\text{el}} = E^\circ_{\text{el}(\text{complex})} - \{E^\circ_{\text{el}(\text{DNA})} + E^\circ_{\text{el}(\text{ligand})}\}$.

Table 1. Comparison of PreDDICTA with Commonly Employed Methods for Scoring/Binding Affinity Prediction

method	brief description	advantages of PreDDICTA	disadvantages of PreDDICTA
Force field Scoring	Comprises van der Waals and electrostatics terms	Includes entropic, solvent, and counterion effects	Computationally slower
Empirical Scoring	Constituent terms, e.g., hydrogen bonding, hydrophobic contacts, rotor terms, desolvation etc. are trained against experimental data; the resultant equation is adopted for scoring	Based on binding phenomenon, thus includes enthalpy and entropy Not trained, hence extensible to other systems	Computationally slower
Knowledge Based Scoring	Frequencies of occurrence of properties like interatomic contacts, pairwise potentials, etc., are determined across large data sets and adopted for scoring	Specific enthalpic and entropic contributions are determined Not trained/derived from data sets, hence extensible to other systems	Computationally slower
MMPBSA/MMGBSA Binding Affinity	Sum of molecular mechanical (MM) terms, solvation electrostatics from Poisson–Boltzmann (PB) or generalized Born (GB) method, solvation van der Waals, and hydrophobicity from solvent accessibility (SA)	Involves a sigmoidal dielectric to account for solvation electrostatics, hence, is computationally swifter	PB or GB methods treat desolvation more rigorously
Linear Interaction Energy, LIE Binding Affinity	Binding affinity calculated from two parameterized terms, where parameters are derived from experimental data and applied on ensemble-averaged energy terms obtained from simulations	Computationally swifter because time intensive simulations are not required May be applied to single structures as well as MD trajectories	Explicit solvent effects not included
Free energy Simulations Binding Affinity	Binding affinity is directly determined via simulation employing techniques, e.g., free energy perturbation and thermodynamic integration	Computationally swifter because time intensive simulations are not required	Lower theoretical rigor Explicit solvent/ion effects not included

groups were considered, simple model building followed by minimization is not expected to reflect the conformation adopted by the ligand in a dynamic environment. Hence, the 34 minimized model-built structures were subjected to nanosecond scale explicit solvent molecular dynamics (MD) simulations. The final structures obtained at the end of each MD simulation were collected and examined for any major structural distortions and deviations from ideal bond, angle, or torsional geometries using NUCHECK,²⁵ available at the RCSB (Protein Data Bank) site.

Thus, a total of 50 structures, comprising 16 energy-minimized crystal structures and 34 processed (minimization and MD) model-built structures were obtained. These structures were evaluated using CURVES²⁴ for DNA structural analysis, and no major deviations from similar DNA–ligand crystal structures were observed. Local inter-base pair parameters for the DNA for all complexes are reported in the Supporting Information. The DNA–ligand binding energy was calculated for each structure using eq 1.

Results and Discussion

The scoring function for DNA–ligand complexes proposed here was guided by our earlier experiences in development of MMGBSA^{6,13,26} and MMPBSA²⁷ and empirical²⁸ approaches

for scoring/binding affinity prediction for protein–DNA,^{26,27} protein–ligand,^{26,28} and DNA–ligand⁶ systems, and we have aimed to capture the theoretical rigor of MMGBSA/MMPBSA methods, as well as the swiftness of simpler empirical/knowledge-based approaches. The former quality is necessary for good binding affinity prediction, while the latter is essential for a scoring function. The resultant of these efforts is an online tool named PreDDICTA (<http://www.scfbio-iitd.res.in/pred-dicta>), which is not aimed to replace any of these approaches, yet presents an attractive alternative in terms of computational speed, binding affinity prediction accuracy, and reliability of underlying theory (Table 1).

Experimentally determined binding free energies and ΔT_m (change in melting temperature of DNA upon drug binding) values are employed for a validation of the proposed computational protocol. The former are a direct measure of binding affinities, while the latter are closely related to binding affinities of DNA–ligand complexes.²⁹ Figure 1a illustrates the linear correlation obtained between the calculated DNA–ligand binding energy and the experimental ΔG° (correlation coefficient,

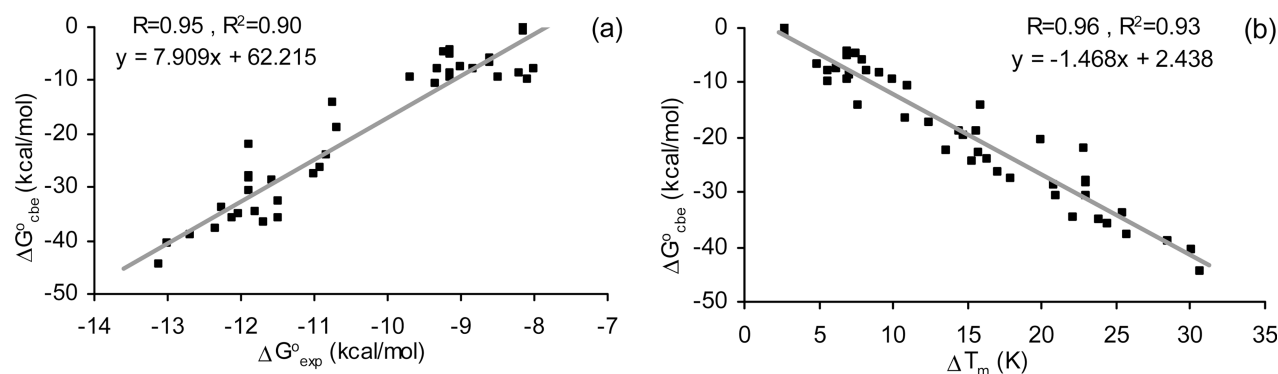


Figure 1. Calculated DNA–ligand binding energy ($\Delta G^\circ_{\text{cbe}}$) versus experimentally determined (a) standard free energies of binding, $\Delta G^\circ_{\text{exp}}$ for 39 complexes, and (b) changes in the melting temperatures of DNA oligomers on ligand binding, ΔT_m for 44 complexes.

$R = 0.95$, $R^2 = 0.90$) for 39 complexes, and Figure 1b shows the correlation ($R = 0.96$, $R^2 = 0.93$) with experimental ΔT_m values for 44 complexes. The high correlations observed despite statistical noise associated with both the theoretical and the experimentally determined quantities indicate the overall stability and viability of the protocol adopted and the utility of this computational tool in a predictive mode.

The energy components, ΔH°_{el} , ΔH°_{vdw} , $T\Delta S^{\circ}_{rt}$, and ΔG°_w computed for each complex are reported in Table S2 in Supporting Information. Direct electrostatics and van der Waals interactions are highly favorable and, though largely compensated by desolvation effects, the overall terms, ΔH°_{el} and ΔH°_{vdw} , remain favorable in almost all cases, in conformity with earlier observations⁶ in DNA–ligand systems. Rotational and translational entropy changes are expectedly unfavorable due to entropy losses on DNA–ligand binding. Release of ordered waters from free DNA and the drug appears to compensate for the entropy loss in reordering of waters around the complex, resulting in overall favorable hydration terms in all cases.

On consideration of each term individually, a moderate correlation of the experimental data is observed with ΔH°_{el} (with ΔG°_{exp} , $R^2 = 0.70$, and ΔT_m , $R^2 = 0.51$), a strong correlation is observed with ΔH°_{vdw} (ΔG°_{exp} , $R^2 = 0.80$; ΔT_m , $R^2 = 0.85$), and no correlation is observed with $T\Delta S^{\circ}_{rt}$ or ΔG°_w . From these observations, one may expect that ΔH°_{vdw} alone or along with ΔH°_{el} would suffice for a binding affinity prediction. However, we consider the inclusion of all four terms in the function necessary for two reasons: first, to maintain theoretical consistency, because they are based on the binding phenomenon, and second, for novel ligands, where entropy could play a stronger role than enthalpy in binding, $T\Delta S^{\circ}_{rt}$ and ΔG°_w would be more significant and their exclusion could lead to erroneous affinity predictions for such ligands.

Further statistical analyses of the energy terms using multiple linear regression indicate the relative weights of each term in the function in the resultant equation,

$$\Delta G^{\circ} = (0.19\Delta H^{\circ}_{el}) + (0.10\Delta H^{\circ}_{vdw}) - (0.19T\Delta S^{\circ}_{rt}) + (0.10\Delta G^{\circ}_w) - 10.08$$

The p values of <0.0001 for ΔH°_{el} and ΔH°_{vdw} , 0.2095 for $T\Delta S^{\circ}_{rt}$, and 0.0052 for ΔG°_w indicate that all four terms affect the correlation with high statistical significance, further supporting the inclusion of all the terms in the energy function. ANOVA analysis results show a very high F value of 106.34 and a correspondingly low p value of <0.0001 , implying that the overall correlation also has high statistical significance (detailed discussion in Supporting Information).

The linear regression equations obtained from the correlations (Figure 1a,b) can be used to predict ΔT_m and ΔG° . This is shown in Table S2 in the Supporting Information, wherein the predicted values are reported alongside the experimental data for comparison. The equations are

$$\Delta G^{\circ}_{pred}(\text{predicted}) = (\Delta G^{\circ}_{cbe} - 62.215)/7.909 \quad (2)$$

$$\Delta T_m(\text{predicted}) = (\Delta G^{\circ}_{cbe} - 2.438)/(-1.468) \quad (3)$$

for binding affinity and ΔT_m prediction, respectively. It may be noted here that this approach differs from using a trained function, because the latter contains coefficients for each term derived from the training data set, while here only the final calculated binding energy is proportionately scaled/converted using the linear regression equation.

The energy function (1) and relations (2) and (3) have been incorporated in PreDDICTA. The tool takes a geometry

optimized structure of the DNA–ligand complex in PDB format as input and proceeds with force field parameter and partial atomic charge assignment, followed by calculation of binding energies (ΔG°_{cbe}) and prediction of ΔT_m and ΔG° . The time taken for energy calculation is 0.05 to 0.20 min, while the complete process, which includes charge derivation (AM1BCC) and parameter assignment, takes 0.08 to 9.00 min on an AMD Opteron processor, depending on the ligand structure, size, and conformation in the complexes in the data set.

It was observed during this study that a few bis-amidinium ligand (i.e., positively charged NH_2CHNH_2 group at both terminals of ligand) DNA complexes do not show conformity to the observed correlation. Experimental data for three complexes of $d(\text{CGCGAATTCGCG})_2$ bound to DAPI (PDB ID: 1D30), Hoechst derivative (311D), and a model-built symmetric bi-benzimidazole derivative (2GXV) indicates very high binding affinity (ΔT_m is 17.1, 32.8, and 22.8 K, respectively), which is underestimated in the calculated binding energies (ΔG°_{cbe} is -6.8 , -23.6 , and -22.1 kcal/mol, respectively). The reason for this is not clear, but it may be due to very strong electrostatic interactions at the amidinium ends, which are not adequately accounted for by the general route of partial atomic charge assignment and electrostatic calculations adopted here and needs system-specific attention. It may also be due to certain phenomena under experimental conditions not reflected in the structure, hence not visible from the calculation. However, it is of interest to note that mono-amidinium containing ligands (2GXJ, 2GXX, 2IRJ, 2GY6, 2GY8, and 2GYE in Table S1 in Supporting Information) bind with affinities that correlate well with those predicted by this energy function.

Independence of the energy function from training on any particular system or structure and the observed strong correlation obtained with experimental data on a dataset of 50 complexes leads to the expectation that not many exceptions may be anticipated when this computational model is employed on any structure outside the data set studied. Also, this data set is fairly diverse structurally, containing mono- as well as dicationic ligands, including seven types of molecules (Supporting Information): bisfuramidines, phenylbenzimidazoles, symmetric and asymmetric substituted bi-benzimidazoles, polyamides, substituted triazene (berenil), and propamidine. The data set also includes six different oligomeric sequences, and though the sequence $d(\text{CGCGAATTCGCG})_2$ dominates, the binding site varies from three to eight base pairs within the set of ligands. The energy function performs well when applied separately on each type of drug in the data set, indicating its extensibility, which is discussed in greater detail in the Supporting Information. Additionally, preliminary results (work in progress) emerging from the application of this tool on 130 protein–ligand complexes indicate a high correlation ($r = 0.88$) between the calculated and experimental binding free energies, strongly supporting the extensibility of the method to systems differing significantly from the data set considered. Further validation and systematic improvements can be envisioned with more diverse ligand structures and DNA sequences as and when the corresponding experimental data is available. As for now, the energy function and the associated computational protocol are expected to perform reasonably well on DNA–ligand complexes, especially when a series of probable drug candidates are to be ranked in terms of their binding affinities.

Conclusions

A computational tool that accounts for diverse energy contributors to DNA–ligand binding affinities at the atomic

level has been developed and tested on 50 DNA–ligand complexes. The correlations obtained between predicted and experimental ΔG° and ΔT_m data are quite satisfactory for the protocol to be harnessed in a predictive mode. The suite of programs for predicting binding affinity and ΔT_m from any input structure of a DNA–ligand complex has been organized as an online tool named PreDDICTA and made freely accessible at <http://www.scfbio-iitd.res.in/preddicta>. The tool has potential value in scoring/binding affinity prediction and assessment of binding properties of newly designed ligands targeted to DNA.

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Supporting Information Available: Citations to original literature on DNA-directed ligands, complex crystal structures, and experimental binding affinity data; calculated energy components, $\Delta G^\circ_{\text{cbe}}$ and ΔT_m values; chemical structures of the ligands studied; DNA structural analysis data for the 50 complexes; detailed discussion on extensibility/generalizability of the method; and results of the multiple regression analysis. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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